

Introduction to Neural Networks & Neural Computation

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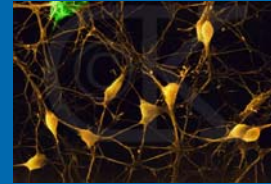
Presentation Overview

- Biological Neurons
- Artificial Neuron Abstractions
- Different types of Neural Nets
 - Perceptron
 - Multi-layer Feed-forward, Error Back-Propagation
 - Hopfield
- Implementation of Neural Nets
 - Chemical & biological systems
 - Computer Software
 - VLSI Hardware
- Alternative Model – Action Potential timing

The Biological Neuron

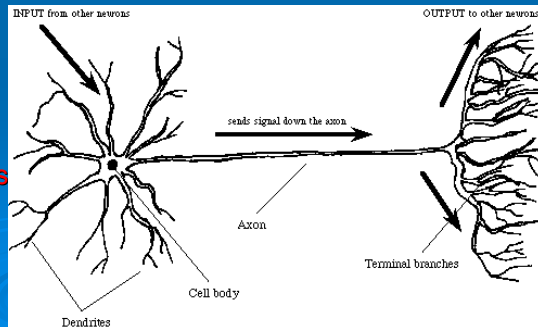
➤ Human Nervous system → 1.3×10^{10} neurons

- 10^{10} are in brain
- Each connected to ~10,000 other neurons
- Power dissipation ~20W



➤ Neuron Structure:

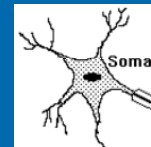
- Cell Body – **Soma**
- **Axon/Nerve Fibers**
- **Dendrites**
- **Presynaptic Terminals**



The Biological Neuron

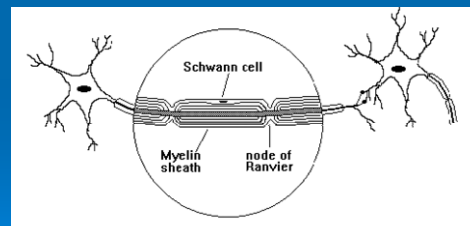
➤ Cell Body – **Soma**

- Includes Nucleus & Perikaryon
- Metabolic Functions
- Generates the transmission signal (*action potential*) – through *axon hillock* -, when received signal threshold reached



➤ **Axon/Nerve Fibers**

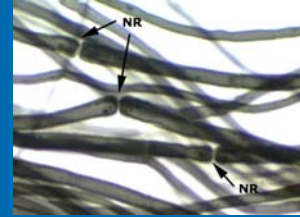
- Conduction Component
- 1 per neuron
- 1mm to 1m
- Extends from axon hillock to terminal buttons
- Smooth surface
- No ribosome



The Biological Neuron

➤ Axon/Nerve Fibers – Myelin Sheath & Nodes of Ranvier

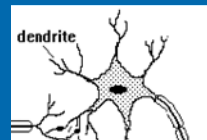
- axons enclosed by **myelin sheath**
→ many layers of **schwann** cells
→ promote axon growth
- Myelin sheath insulates axon from extracellular fluid:
thicker myelin → faster propagation
- Myelin sheath gaps: **Nodes of Ranvier**
→ Depolarization occurs sequentially
→ trigger next node → impulse propagates to next
hop & restored at each node (buffering)



The Biological Neuron

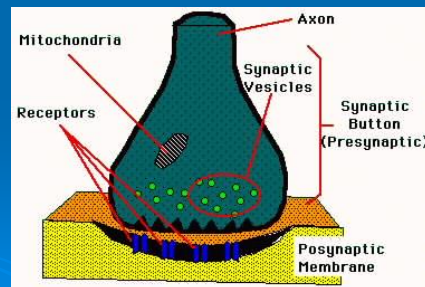
➤ Dendrites

- The receiver / input ports
- Several Branched
- Rough Surface (dendritic spines)
- Have ribosomes
- No myelin insulation



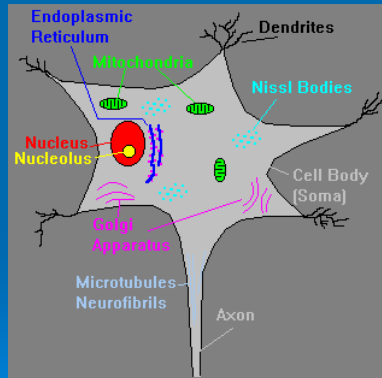
➤ Presynaptic Terminals

- The branched ends of axons
- Transmit the signal to other
neurons' dendrites
with *neurotransmitters*



The Biological Neuron

➤ Inside of a Neuron:

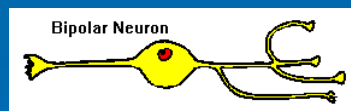
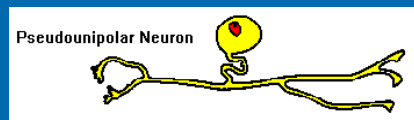


- **Nucleus** - genetic material (chromosomes)
- **Nucleolus** - Produces ribosomes : genetic information → proteins
- **Nissl Bodies** - groups of ribosomes → protein synthesis
- **Endoplasmic reticulum (ER)** - system of tubes → material transport in cytoplasm
- **Golgi Apparatus** - membrane-bound structure → packaging peptides and proteins (including neurotransmitters) into vesicles
- **Microfilaments/Neurotubules** - transport for materials within neuron & structural support.
- **Mitochondria** - Produce energy

The Biological Neuron

➤ Neuron Types:

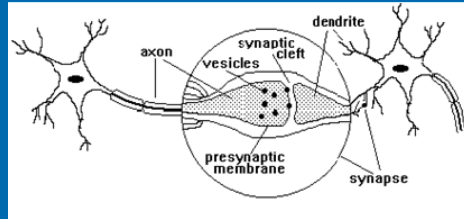
- Unipolar Neuron
 - One process from soma → several branches
 - 1 axon, several dendrites
 - No dendrites from soma
- PseudoUnipolar Neuron
 - 2 axons
- Bipolar Neuron
 - 2 processes from soma
 - (PseudoUnipolar ← bipolar)
- Multipolar Neuron
 - Single axon
 - Several dendrites from soma



The Biological Neuron

> Synapse:

- Junction of 2 neurons
- Signal communication
- Two ways of transmission:
 - Coupling of **ion channels** → Electrical Synapse
 - Release of chemical transmitters → Chemical Synapse



> Chemical Synapse:

- Presynaptic neuron releases **neurotransmitters** through **synaptic vesicles** at terminal button to the **synaptic cleft** – the gap between two neurons.
- Dendrite receives the signal via its receptors
- [Excitatory & Inhibitory Synapses – Later]

The Biological Neuron

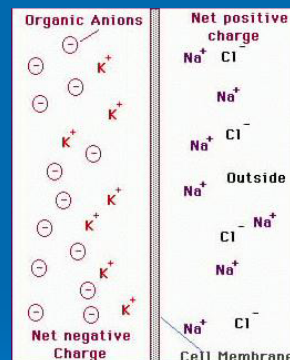
> Membrane Potential:

- 5nm thick, semipermeable
- Lipid bilayer controls ion diffusion
- Potential difference ~70 mV
- Charge pump:
 - $\text{Na}^+ \rightarrow$
 - $\leftarrow \text{K}^+$



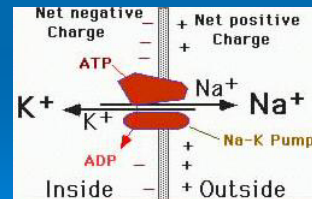
> Resting Potential:

- When no signaling activity
- Outside potential defined 0
 - → $V_r = \sim -70\text{mV}$



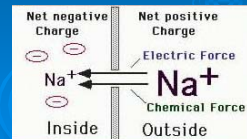
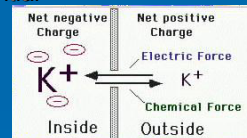
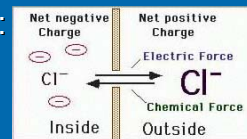
The Biological Neuron

- Membrane Potential – Charge Distribution:
 - Inside: More K^+ & Organic Anions (acids & proteins)
 - Outside: More Na^+ & Cl^-
 - 4 Mechanisms that maintain charge distribution = membrane potential:
 - 1) Ion Channels:
 - Gated | Nongated
 - Selective to specific ions
 - Ion distribution \leftarrow channel distribution
 - 2) Chemical Concentration Gradient
 - Move toward low gradient
 - 3) Electrostatic Force
 - Move along/against E-Field
 - 4) **Na-K Pumps**
 - Move Na & K against their net electrochemical gradients
 - Requires Energy \rightarrow ATP Hydrolysis (ATP \rightarrow ADP)



The Biological Neuron

- Membrane Potential – Charge Distribution:
 - Cl^- :
 - Concentration gradient \leftarrow
 - Electrostatic Force \rightarrow
 - Final concentration depends on membrane potential
 - K^+ :
 - Concentration gradient \rightarrow
 - Electrostatic Force \leftarrow
 - Na-K pump \leftarrow
 - Na^+ :
 - Concentration gradient \leftarrow
 - Electrostatic Force \leftarrow
 - Na-K pump \rightarrow

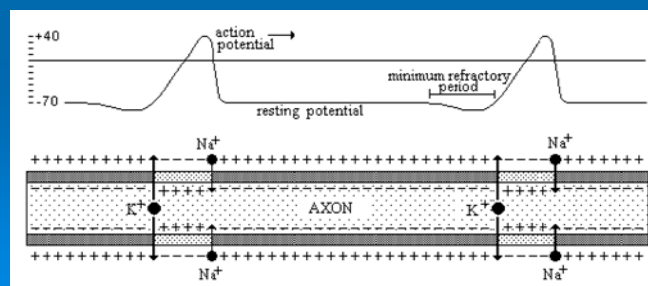


The Biological Neuron

- Excitatory & Inhibitory Synapses:
 - Neurotransmitters → Receptor sites at postsynaptic membrane
 - Neurotransmitter types
 - Increase Na-K pump efficiency
 - → [Hyperpolarization](#)
 - Decrease Na-K pump efficiency
 - → [Depolarization](#)
 - **Excitatory Synapse:**
 - Encourage depolarization
 - ← Activation decreases Na-K pump efficiency
 - **Inhibitory Synapse:**
 - Encourage hyperpolarization
 - ← Activation increases Na-K pump efficiency

The Biological Neuron

- Action Potential:
 - Short reversal in membrane potential
 - → Current flow: Action Potential → Rest Potential
 - → Propagation of the depolarization along axon



The Biological Neuron

➤ Action Potential:

- Sufficient Excitatory Synapses Activation – Depolarization of Soma

→ trigger action potential:

- Some Voltage gated Na Channels open
 - Membrane Na Permeability Increases
 - $\leftarrow \text{Na}^+ \rightarrow$ Depolarization increases
- Depolarization builds up exponentially...

Positive Feedback



The Biological Neuron

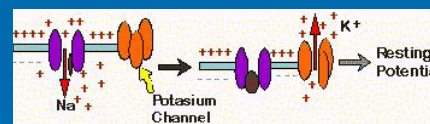
➤ Action Potential:

- Cl^- : Electrostatic Force ' \rightarrow ' decreases
 - more $\text{Cl}^- \leftarrow$
- K^+ : Electrostatic Force ' \leftarrow ' decreases
 - more $\text{K}^+ \rightarrow$
- These cannot cease depolarization

➤ Repolarization:

- Termination of action potential
- 2 Processes:

- Inactivation of Na Channels
 - Na channels have 2 types of gating mechanisms:
 - Activation during depolarization → open Na Channels
 - Inactivation after depolarization → close Na Channels
- Delayed Activation of Voltage gated K Channels
 - → more $\text{K}^+ \leftarrow$ → more $\text{Na}^+ \rightarrow$



The Biological Neuron

- Action Potential – Complete Story:
 - Neurotransmitters → Dendrites Receptors
 - ➔ Initiate synaptic potential
 - Potential spreads toward initial axon segments
 - Passive excitation – no voltage gated ion channels involved
 - Action potential initiation at axon hillock
 - ← highest voltage gated ion channel concentration
 - Happens if arriving potential > voltage gated channel threshold
 - Wave of depolarization/repolarization propagates along axon
 - Turns on transmission mechanisms at axon terminal
 - Electrical or Chemical Synapse



The Biological Neuron

- Refractory Period:
 - Once an action potential passes a region, the region cannot be reexcited for a period ~1ms
 - Depolarized parts of neuron recover back to resting potential ← Na-K pumps
 - Max pulse rate ~1Khz
 - ➔ Electrical pulse propagates in a single direction
 - Inverse hysteresis?
 - Mexican wave
 - Electrical signals propagate as *pulse trains*

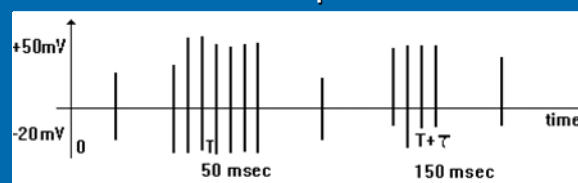
The Biological Neuron

➤ Pulse Trains:

- Non-digital signal transmission nature
- Intensity of signal → frequency of pulses
 - Pulse Frequency Modulation
- Almost constant pulse amplitude
- Neuron can send pulses arbitrarily even when not excited!
 - Much Less Frequency - Noise

The Biological Neuron

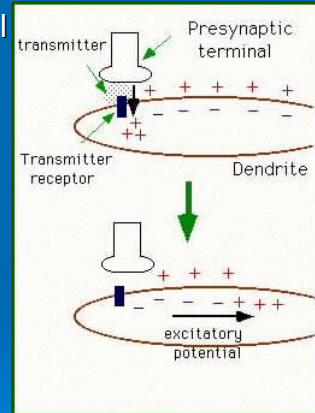
➤ Pulse Trains - Example:



- $t=0 \rightarrow$ Neuron Excited
- $t=T$ [$\sim 50\text{ms}$] \rightarrow Neuron fires a train of pulses
- $t=T+\tau \rightarrow$ Neuron fires a second set of pulses Due to first excitation
 - Smaller # of pulses
- Neuron sends random less frequent pulses

Biological Neuron: Processing of Signals

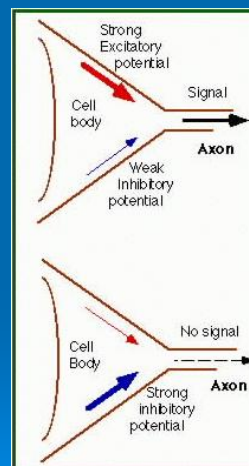
- A cell at rest maintains an electrical potential difference known as the resting potential with respect to the outside.
- An incoming signal perturbs the potential inside the cell. Excitatory signals depolarizes the cell by allowing positive charge to rush in, inhibitory signals cause hyperpolarization by the in-rush of negative charge.



<http://www.ifisiol.unam.mx/Brain/neuron2.htm>

Biological Neuron: Processing of Signals

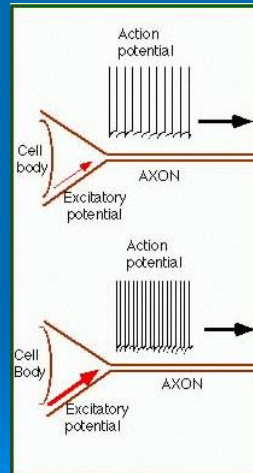
- Voltage sensitive sodium channels trigger possibly multiple “action potentials” or voltage spikes with amplitude of about 110mV depending on the input.



<http://www.ifisiol.unam.mx/Brain/neuron2.htm>

Biological Neuron: Conduction in Axon

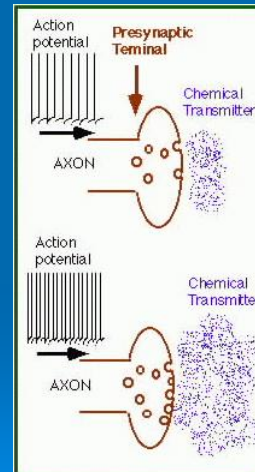
- Axon transmits the action potential, regenerating the signal to prevent signal degradation.
- Conduction speed ranges from 1m/s to 100m/s. Axons with myelin sheaths around them conduct signals faster.
- Axons can be as long as 1 meter.



<http://www.ifisiol.unam.mx/Brain/neuron2.htm>

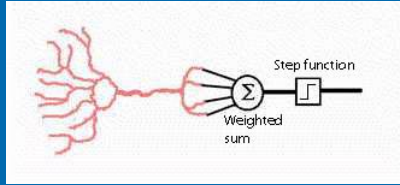
Biological Neuron: Output of Signal

- At the end of the axon, chemicals known as neurotransmitters are released when excited by action potentials.
- Amount released is a function of the frequency of the action potentials. Type of neurotransmitter released varies by type of neuron.




<http://www.ifisiol.unam.mx/Brain/neuron2.htm>

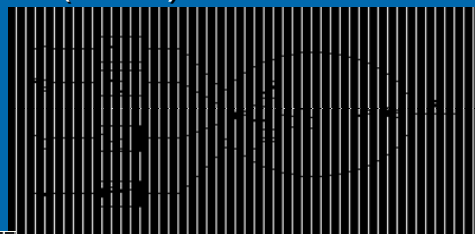
Artificial Neuron Abstraction



- Neuron has multiple inputs
- Inputs are weighted
- Neuron “fires” when a function of the inputs exceed a certain threshold
- Neuron has multiple copies of same output going to multiple other neurons

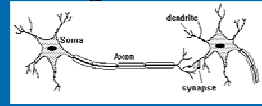
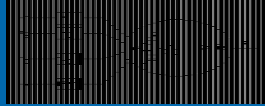
Artificial Neuron Abstraction

- McCulloch-Pitts Model (1943)
 - I/p:s:[$u_1 \dots u_N$]
 - Weights:[$w_1 \dots w_N$]
 - θ : Threshold/bias
 - $\theta < 0 \rightarrow$ Threshold
 - $\theta > 0 \rightarrow$ Bias
 - Activation: 
 - O/p: x
 - O/p function/Activation function: $x=f(a)$



Artificial Neuron Abstraction

➤ McCulloch-Pitts Model vs. Biological Neuron



- I/ps ⇔ Electrical signals received at dendrites
 - Amplitude ⇔ Amount of Neurotransmitters ← Pulse Frequency
 - + ⇔ Excitatory & - ⇔ inhibitory
- Weights ⇔ Synaptic strength
Dendrite receptors
- θ ⇔ Resting Potential
 - $\theta < 0$ always in neuron
- Activation ⇔ Sum of all synaptic excitations + resting potential
- Activation Function ⇔ Voltage gated Na Channel Threshold function
- O/p ⇔ Action potential initiation/repression at axon hillock

Artificial Neuron Abstraction

➤ McCulloch-Pitts Model – Formulation

- Activation
- Augmented weights
 - $u_0=1$ & $w_0= \theta$
- Vector Notation
- O/p function
 - Threshold
 - Ramp
 - Sigmoid



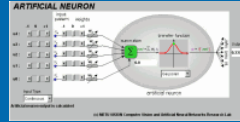
$$f(x) = \frac{1}{1 + e^{-\beta x}}$$



Artificial Neuron Abstraction

➤ McCulloch-Pitts Model – Example

- 4 I/p neuron →

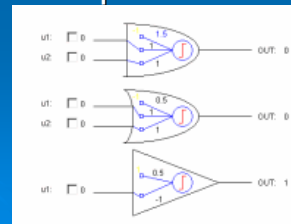


➤ McCulloch-Pitts – Logic Gate Implementation

1	0	1	1	1	1	1	1	0
0	0	0	0	0	1	0	1	0
AND	0	1	OR	0	1	NOT	0	1

- XOR? –linear separation!

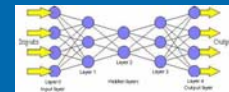
1	1	0
0	0	1
XOR	0	1



Neural Network Types

➤ Feedforward

- (Multicategory) Perceptron
- Multilayer – Error Backpropagation



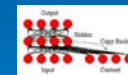
➤ Competitive

- Hemming
- Maxnet

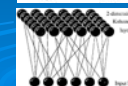


➤ Variations of Competitive

- Adaptive Resonance Theory (ART)
- Kohonen



➤ Hopfield



Hopfield Networks

- First developed by John Hopfield in 1982
- Content-Addressable Memory
- Pattern recognizer
- Two Types: Discrete and Continuous
- Common Properties:
 - Every neuron is connected to every other neuron. Output of neuron i is weighted with weight w_{ij} when it goes to neuron j .
 - Symmetric weights: $w_{ij} = w_{ji}$
 - No self-loops: $w_{ii} = 0$
 - Each neuron has a single input from the outside world

Discrete Hopfield Network: Training / Initialization

- Training: (Storing bipolar patterns)
 - Simultaneous, Single-step
 - Patterns: $s(p) = \{s_1(p), s_2(p), \dots, s_n(p)\}$
 - Weight Matrix $W = \{w_{ij}\}$

$$T_{ij} = \sum_p s_i(p) * s_j(p) \text{ for } i \neq j$$

Fausett, Laurene. *Fundamentals of Neural Networks: Architectures, Algorithms and Applications*. Prentice Hall, Englewood Cliffs, NJ, 1994.

Discrete Hopfield Networks: Execution / Pattern Recall

- Asynchronous update of neurons
 - Neurons are updated sequentially at random
- Compute net input: $V_{in_i} = I_i + \sum_j V_j * T_{ji}$
- Determine activation/output:

$$V_i = \begin{cases} 1 & \text{if } V_{in_i} > \theta_i \\ V_i & \text{if } V_{in_i} = \theta_i \\ 0 & \text{if } V_{in_i} < \theta_i \end{cases}$$

- Broadcast output V_i to all other neurons.

Hopfield, J.J. "Neurons with graded response have collective computational Properties like those of two-state neurons" in Proc.Natl.Acad.Sci, USA, Vol.81, pp3088-3092

Discrete Hopfield Network

- Binary Hopfield Network Demo:



<http://www.techhouse.org/~dmorris/JOHN/StinterNet.html>

Discrete Hopfield Networks: Proof of Convergence

- Output of neuron i:

$$V_i = \begin{cases} 1 & \text{if } \sum_{j \neq i} T_{ij} V_j > \theta_i \\ V_i & \text{if } \sum_{j \neq i} T_{ij} V_j = \theta_i \\ 0 & \text{if } \sum_{j \neq i} T_{ij} V_j < \theta_i \end{cases}$$

- Consider the following Energy function:

$$E = -\frac{1}{2} \sum_j \sum_{i \neq j} T_{ij} V_i V_j - \sum_i I_i V_i + \sum_i \theta_i V_i$$

This implies...

$$\Delta E = - \left[\sum_{i \neq j} T_{ij} V_i + I_i - \theta_i \right] [\Delta V_i] \leq 0$$

because $[\]$ always has the same sign

Hopfield, J.J. "Neurons with graded response have collective computational Properties like those of two-state neurons" in Proc.Natl.Acad.Sci, USA, Vol.81, pp3088-3092

Discrete Hopfield Networks: Proof of Convergence (2)

- Furthermore, the energy function is bounded...since T_{ij} 's are all fixed, V_i is either V_0 or V_1 (typically 1 or 0), and θ_i 's are also fixed.

$$E = -\frac{1}{2} \sum_j \sum_{i \neq j} T_{ij} V_i V_j - \sum_i I_i V_i + \sum_i \theta_i V_i$$

- Since $\Delta E \leq 0$ and E is bounded, the system must eventually settle down at a local or global minimum in terms of E .

Continuous Hopfield Networks

- **Continuous values for neuron states** and outputs instead of discrete binary or bipolar values.
- **Simultaneous update** instead of serial asynchronous update of discrete network
- **Chemical system** can emulate continuous hopfield nets

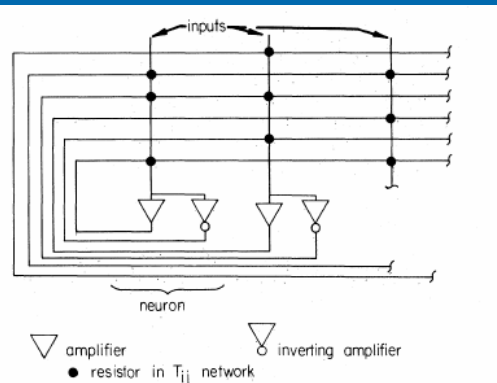
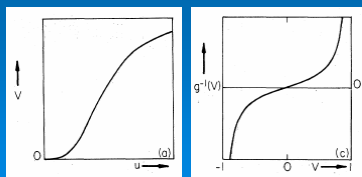
Continuous Hopfield Networks How do they work?

- Can be modeled as the following electrical system:

$$C \left(\frac{dv}{dt} \right) = \frac{dQ}{dt} = I$$

$$C_i \left(\frac{du_i}{dt} \right) = \sum_j T_{ij} V_j - \frac{u_i}{R_i} + I_i$$

$$u_i = g_i^{-1}(V_i)$$



Continuous Hopfield Networks Proof of Convergence

- Consider the following Energy Function:

$$E = -\frac{1}{2} \sum_i \sum_j T_{ij} V_i V_j + \sum_i \frac{1}{R_i} \int_0^{V_i} g_i^{-1}(V) dV + \sum_i I_i V_i$$

- Its time derivative with a symmetric T:

$$\frac{dE}{dt} = -\sum_i \frac{dV_i}{dt} \left(\sum_j T_{ij} V_j - \frac{u_i}{R_i} + I_i \right)$$

Hopfield, J. J. "Neurons with graded response have collective computational properties like those of two-state neurons", Proceedings of the National Academy of Science, USA, Vol 81, pp. 3088-3092, May 1984, Biophysics.

Continuous Hopfield Networks Proof of Convergence

- The bracket inside the time derivative of the energy function is the same as that in the original function describing the system.

$$\frac{dE}{dt} = -\sum_i \frac{dV_i}{dt} \left(\sum_j T_{ij} V_j - \frac{u_i}{R_i} + I_i \right) \quad C_i \left(\frac{du_i}{dt} \right) = \sum_j T_{ij} V_j - \frac{u_i}{R_i} + I_i$$

$$\frac{dE}{dt} = -\sum_i C_i \left(\frac{dV_i}{dt} \right) \left(\frac{du_i}{dt} \right)$$

$$= -\sum_i C_i g_i^{-1}(V_i) \left(\frac{dV_i}{dt} \right)^2 \leq 0, \quad \frac{dE}{dt} = 0 \Rightarrow \frac{dV_i}{dt} = 0 \text{ for } \forall i$$

Hopfield, J. J. "Neurons with graded response have collective computational properties like those of two-state neurons", Proceedings of the National Academy of Science, USA, Vol 81, pp. 3088-3092, May 1984, Biophysics.

Chemical Implementation of Neural Networks

➤ Single Chemical Neuron i:

- $I_{1i}^* + C_i \leftrightarrow X_{1i} + C_i$ $J_{1i} = k_1 C_i - k_{-1} C_i K_{1i}$
- $X_{1i} + B_i \leftrightarrow X_{2i}^* + A_i$ $J_{2i} = k_2 X_{1i} B_i - k_{-2} A_i$

➤ C_i is the Input

➤ $A_i + B_i = \text{constant}$

- A_i is high, B_i is low if C_i is above threshold
- B_i is high, A_i is low if C_i is below threshold

Hjelmfelt, Allen, et al. "Chemical Implementation of neural networks and Turing machines"
 Proceedings of the National Academy of Science, USA. Vol 88, pp10983-10987, Dec. 1991

Chemical Implementation of Neural Networks

➤ Construction of Interneuronal Connections:

- Species A_i and B_i may affect the concentration of the catalyst C_j of other neurons

$$C_j = \sum_k C_{jk}$$

➤ Each neuron uses a different set of chemicals and occupy the same container

- Similar to logic networks using gene networks

Chemical Implementation of Neural Networks: AND gate

- A_i and A_j are output

Computing with Action Potential Timing

- [Alternative to Neural Network Communication Model]
- Neurons communicate with action potentials →
- Engineering models for neuron activity use continuous variables to represent neural activity
 - Activity → <rate of action potential generation>
- Traditional neurobiology: same model →
 - “short term mean firing rate”
- Average pulse rate is inefficient in neurobiology
 - Single neuron → Wait for several pulses → slow
 - Multiple equivalent neurons → average over → redundant ‘wetware’ & error

Action Potential Timing

- New examples in Biology:
 - Information → Timing of action potentials (Rather than pulse rate)
 - Ex: Moustache Bat
 - Uses timing to discriminate its sonar from environmental noise
 - Application: Analog match of odour identification
 - Solved more efficiently using action potential timing

Action Potential Timing

- Moustache Bat Sonar:
 - Generates 10 ms ultrasonic pulse with frequency increasing with time ('chirp')

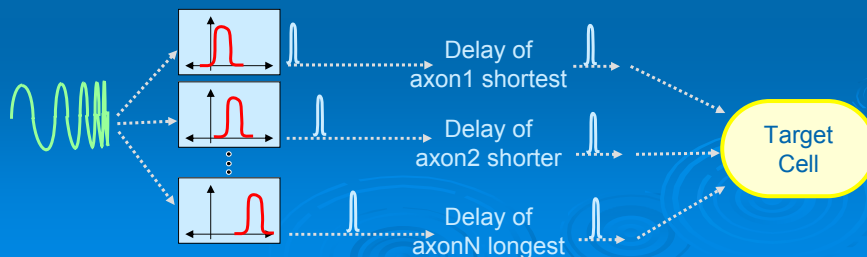


- Chirp is received back in cochlea

Action Potential Timing

➤ Moustache Bat Sonar:

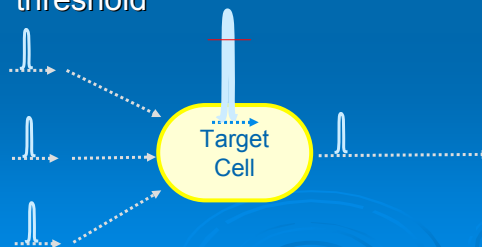
- In cochlea, cells with different freq. Selectivity (Filter bank)
 - Produce a single action potential if signal is within the pass-band
 - No action potential otherwise
 - Sequential response to different frequencies



Action Potential Timing

➤ Moustache Bat Sonar:

- Pulses leave cochlea cells in order
- Length and propagation speeds of axons different → all pulses arrive at target cell simultaneously
- High aggregate action potential at target cell reaches threshold



Action Potential Timing

➤ Analog match

- Odour → Mixture of molecules with different concentrations: N_i $odour_b: \bigcup_i N_i^b$

- Matching odour

- Intensity () varies
- Concentration ratios similar

- → normalized concentrations n_i similar: (λ : intensity)

$$n_i^b = \frac{N_i^b}{\lambda \left(= \sum_j N_j^b \right)}$$

- **Analog match:**

- Whether stimulus, s , has the similar concentration ratios of constituents to a prescribed target ratio $n_1: \dots : n_i: \dots : n_k$

- Formulation: $\exists \lambda : \forall N_j \in s; N_j^s \approx \lambda \cdot n_j^b$

- Conceptually:

- Similarity of ratios (N1:N2:...:Nk)
- Similarity of vector direction



Action Potential Timing

➤ Analog Match – Neural network implementation:

- Unknown odour vector I : $[I_1 \ I_2 \ \dots \ I_k]$

- Check if matches $normalized_odour_b: \bigcup_i \{n_i^b\}$

- Target odour vector n :

$$n = \begin{bmatrix} n_1 \\ n_2 \\ \vdots \\ n_k \end{bmatrix}$$

- Define weight vector W :

$$W = \frac{n}{\|n\|}$$

- Normalize I to unit length vector:

$$I_{norm} = \frac{I}{\|I\|}$$

- Recognition:

$$\vec{I}_{norm} \cdot \vec{W} > threshold (i.e. 0.95)$$

- Result of inner product →

- $\cos(I_{norm}, W) \rightarrow [-1, 1]$; actually $[0, 1]$ as both vectors in 1st quadrant (concentrations > 0)
- Closer to 1 → vectors align better

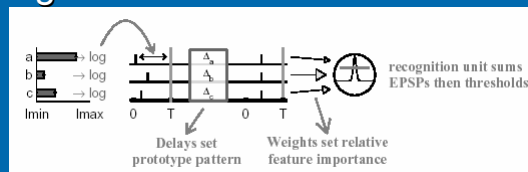
Action Potential Timing

➤ Analog Match – Neural network implementation:

- 4 weaknesses:
 - Euclidean normalization expensive
 - If weak component (in conc.) has importance or strong is unreliable, we cannot represent this – weights describe only concentration of comp-s
 - We can have ‘weighted’ weights
[w1]: conc. Ratios & [w2]: priorities → $W=w1.*w2$
 - No Hierarchical design → normalization problem
 - No tolerance to missing i/ps or highly wrong i/ps
 - I.e. $n1:n2:n3:n4:n5$ 1:7:1.5:0.4:0.1 (/10)
 - > {1,1,2,1,3,1,4,1,5}: {1, 0, 1.5, 0.4, 0.1}
 - > {1,1,2,1,3,1,4,1,5}: {1, 7, 9, 0.4, 0.1}

Action Potential Timing

➤ Analog match – Action Potential Method



- 3 i/ps l_a, l_b, l_c → $\log(l_x)$ define advance before reference time T
- Target odour in $[n]$ → $n = \begin{bmatrix} n_a \\ n_b \\ n_c \end{bmatrix}$
 - Delays: $\Delta_j = \log(n_j)$
 - ! $[n]$ should be upscaled to have $n_i > 1$ (o/w advancer!)
- Analog Match →
All pulses arrive at target simultaneously
 - Scaling doesn't change relative timing – all shift

$$\log(\lambda \cdot I_x) = \log(I_x) + \log(\lambda)$$

Action Potential Timing

➤ Analog match – Action Potential Method

- Ex:

$$n = \begin{bmatrix} n_a \\ n_b \\ n_c \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \Rightarrow \begin{array}{l} \Delta_a = \log(n_a) = 0 \\ \Delta_b = \log(n_b) = 0.31 \\ \Delta_c = \log(n_c) = 0.48 \end{array}$$

$$I = [I_a \ I_b \ I_c] = [10 \ 20 \ 30] \Rightarrow \text{Perfect Match}$$

$$\log(I) = [1 \ 1.31 \ 1.48] \Rightarrow$$

$$\left. \begin{array}{l} I_a \text{ starts at: } T-1 \\ I_b \text{ starts at: } T-1.31 \\ I_c \text{ starts at: } T-1.48 \end{array} \right\} \begin{array}{l} I_a \text{ ends at: } T-1+0=T-1 \\ I_b \text{ ends at: } T-1.31+0.31=T-1 \\ I_c \text{ ends at: } T-1.48+0.48=T-1 \end{array}$$

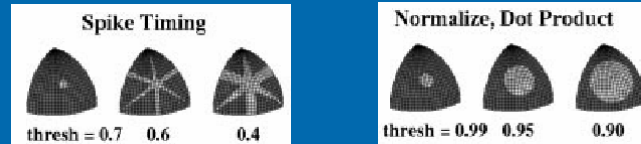
Action Potential Timing

➤ Analog match – Action Potential Method

- All 4 weaknesses removed
- (1) No normalization required
- (2) Pulse advances w.r.t. T
 - concentration/scaling
 - Synaptic Weights → importance
- (3) Hierarchy can exist
 - all neurons independent
- (4) Tolerates missing/grossly inaccurate info
 - ⇒

Action Potential Timing

- Analog match
- Error Tolerance Comparison of 2 Methods:
 - Target = $n = [1 \ 1 \ 1]^T$



- Neural Net Model →
 - The cone around $[1 \ 1 \ 1]$ vector defines tolerance: projects a ~circle on unit circle
- Action Potential Timing → makes bisectors → star shape
 - Finds individual scalings: pulses with same scaling overlap
- Received $I/p = I = [1 \ 1 \ 0]^T$ →
 - Neural net needs to accept almost every i/p
 - Action potential timing detects similarity

Action Potential Timing

- Analog match – Action Potential Method
 - Reference Time T
 - Reference time T known by all neurons
 - Externally generated → bat example
 - Internally generated periodically

Neural Network Hardware: TOTEM

➤ Developed by



Neural Network Hardware: IBM ZISC



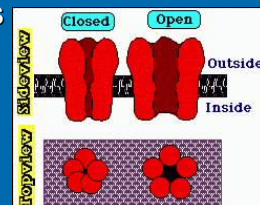
Index of Terms

- **Perikaryon:** body of a nerve cell as distinguished from the nucleus, axon, and dendrites [Back](#)
- **axon hillock:** a specialized region of the soma called the axon hillock where the action potential is initiated once a critical threshold is reached [Back](#)
- **terminal buttons:** The larger ends of axons at the synapse, where the neurotransmitters are released – same as presynaptic terminals [Back](#)

Index of Terms

- **Ion channels :** specialized cellular devices that can transport ions in and out of the cell thru the membrane [Back](#)

- **Nongated channels** are always open and are not influenced significantly by extrinsic factors
- **Gated channels** open and close in response to specific electrical, mechanical, or chemical signals



- **Neurotransmitters:** small molecules that are liberated by a presynaptic neuron into the synaptic cleft and cause a change in the postsynaptic membrane potential [Back](#)

Index of Terms

- **Depolarization** : Reduction of membrane charge separation = Increase in Membrane potential (less negative) [Back](#)
- **Hyperpolarization** : Increase in membrane charge separation = Decrease in Membrane potential (more negative) [Back](#)
- **Neurotransmitters**: small molecules that are liberated by a presynaptic neuron into the synaptic cleft and cause a change in the postsynaptic membrane potential [Back](#)